# Lecture 6 Assessing the Completeness of Death Registration Multiple Census Methods

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#### Outline

- Generalized Growth Balance (GGB) method
- Synthetic Extinct Generation (SEG) method

## Data Requirements and assumptions for both methods

- Data requirements for both methods
  - Age distribution of population at two successive censuses
  - · Age distribution of deaths for intercensal period
- Assumptions
  - Coverage of each census is the same for all ages
  - Completeness of reporting of deaths is the same for all ages from a minimum age (usually age 15)
  - The population is closed to migration (or information on migration is available)
  - No assumption of stability

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#### Generalized Growth Balance Method - theory

- Recall from Brass Growth Balance method
- In any closed population, between time t1 and t2:
  - CGR = CBR CDR (or r = b d)
- This expression also holds for open-ended age segments x+, deaths being the deaths at ages x and over, "births" being birthdays at age x, and the denominators being the population aged x and over
  - r(x+) = b(x+) d(x+)
    - b(x+) = N(x)/N(x+)
    - d(x+) = D(x+)/N(x+)
  - b(x+) r(x+) = d(x+)

#### Generalized Growth Balance Method - theory

- Assume that deaths are registered with a completeness c, constant at all ages: d<sup>r</sup>(x+)=d(x+)\*c
  - d(x+) = true death rate at ages x+
  - dr(x+) = recorded death rate at ages x+
- $d(x+) = d^r(x+)/c$
- $b(x+) r(x+) = \{1/c\} * d^r(x+)$
- If we can estimate b(x+) and r(x+) from census data, there should exist a linear relation between the residual (b(x+) r(x+)) and the direct estimate of the death rate  $d^r(x+)$ . The slope of the line should estimate  $\{1/c\}$ , the coverage of deaths.

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#### Generalized Growth Balance Method - theory

The expression

$$b(x+) - r(x+) = {1/c}*d^{r}(x+)$$

is the equation of a straight line, slope 1/c, but no intercept term (i.e. passes through the origin).

• In practice, observed points may indicate that the relation does not pass through the origin. This indicates that the two censuses may have different completeness.

#### Generalized Growth Balance Method - theory

- Assume the coverage of the first census is k1
- Assume the coverage of the second census is k2
- Assume coverage is constant with age.
- Then equation becomes:

$$b(x+) - r(x+) = \frac{\ln(k_1/k_2)}{t_2 - t_1} + \frac{\sqrt{k_1 k_2}}{c} d^r(x+)$$

• Estimate b(x+), r(x+) and  $d^r(x+)$  from data. Estimate intercept a and slope b of equation using linear regression. Completeness c can be derived from a and b.

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# Generalized Growth Balance Method – Data Requirements

- Number of women (men), by five year-age group, and for open age interval A+ (with A as high as possible), at two points in time, typically from the results of two censuses.
- Number of deaths of women (men), by five-year age group, and for open age interval A+, over the period between the two censuses.

### Generalized Growth Balance Method - steps

- Step 1: Estimate the number of deaths reported in the period between the two census.
  - Apportion annual deaths in the first and last year of the census
- Example: Suppose census dates are April 1, 2000 and April 1, 2010. Then intercensal deaths are:

$$.75*_{5}D_{x}(2000) + {}_{5}D_{x}(2001) + {}_{5}D_{x}(2002) + ... + {}_{5}D_{x}(2009) + .25*_{5}D_{x}(2010)$$

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#### Generalized Growth Balance Method - steps

- Step 2: Cumulate population and deaths downwards
- Population:  $N(x+) = \sum_{y=x}^{A-5} {}_5N_y + {}_\infty N_A$
- Same for deaths D(x+)

#### Generalized Growth Balance Method - steps

• Step 3: Calculate the Person-Years of life lived, PYL(x+)

$$PYL(x +) = (t_2 - t_1) (N(x +, t_1) \times N(x +, t_2))^{\frac{1}{2}}$$

• Step 4: Calculate the number of people who turned x in the population, N(x)

$$N(x) = \frac{t}{5} \left( {}_{5}N_{x-5}(t_1) \times {}_{5}N_x(t_2) \right)^{\frac{1}{2}}$$

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#### Generalized Growth Balance Method - steps

• Step 5: Calculate b(x+), d(x+) and r(x+) 
$$b(x+) = \frac{N(x)}{PYL(x+)}$$

$$d(x+) = \frac{D(x+)}{PYL(x+)}$$

$$r(x+) = \frac{{}_{\infty}N_{\chi}(t_2) - {}_{\infty}N_{\chi}(t_1)}{PYL(x+)}$$

## Generalized Growth Balance Method - steps

- Step 6: Plot graph of b(x+)-r(x+) against d(x+)
- Step 7: Fit line, estimate a and b, and then c
  - If intercept *a* is negative:

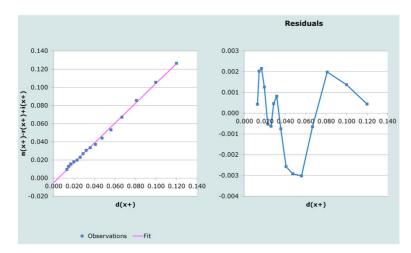
$$c = \frac{e^{a(t_2 - t_1)}}{b}$$

• If intercept *a* is positive:

$$c = \frac{e^{-a(t_2 - t_1)}}{b}$$

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## Example: South Africa, Males, 2001-07



Intercept a = -.00467 Slope b = 1.0907

Completeness c = .9175 = **92%** 

#### Limitations

- Migration
- Fluctuation of completeness of death registration by age

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## Synthetic Extinct Generation method - theory

- Extension of the Preston and Coale method for populations that are not stable and for which two censuses are available.
- In a stable population:

$$N(80,t) = D(80,t) + D(81,t) \times e^r + D(82,t) \times e^{2r} + \dots$$

• In any closed population:

$$N(80,t) = D(80,t) + D(81,t) \times e^{\,_1r_{80}} + D(82,t) \times e^{\left(\,_1r_{80} + \,_1r_{81}\right)} + \, \dots$$

where  $_1r_x$  is the growth rate of the population aged x, x+1

#### Synthetic Extinct Generation method - theory

- In reality we have  $D_a^r$  (=recorded deaths) rather than  $D_a$  (=true deaths)
- If deaths are not completely recorded, then  $D_a^r = c^*D_a$ , or  $D_a = D_a^r/c$
- If we use  $D_a^r$  instead of  $D_a$  when summing deaths, we obtain  $\widehat{N}_x$  instead of the true population  $N_x$
- The ratio  $\frac{\widehat{N}_{x}}{N_{x}}$  gives an estimate of completeness c

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# Generalized Growth Balance Method – Data Requirements

- Number of women (men), by five year-age group, and for open age interval A+ (with A as high as possible), at two points in time, typically from the results of two censuses.
- Number of deaths of women (men), by five-year age group, and for open age interval A+, over the period between the two censuses.

#### Synthetic Extinct Generation method - steps

- Step 1: Estimate the number of deaths reported in the period between the two census.
  - Apportion annual deaths in the first and last year of the census
- Step 2: estimate age-specific growth rates between the two censuses, adjusted for change in census coverage

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$$_{5}r_{x} = \frac{ln(_{5}N_{x}(t_{2})/_{5}N_{x}(t_{1}))}{t_{2}-t_{1}} + \delta$$

•  $\delta$  = intercept  $\alpha$  estimated in Generalized Growth Balance method

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#### Synthetic Extinct Generation method - steps

- Step 3: Estimate life expectancy at age A and five-year age intervals down to 65
  - Use estimates from Generalized Growth Balance method (or other sources if available)

#### Synthetic Extinct Generation method - steps

• Step 4: Estimate the number of people who turned x, and the number of people aged x, x+5, from the reported deaths

$$egin{aligned} \widehat{N}_x &= \widehat{N}_{x+5} \exp ig( 5_5 r_x ig) + {}_5 D_x \exp ig( 2.5_5 r_x ig) \ \\ \widehat{N}_A &= {}_\infty D_A ig( \exp ig( {}_\infty r_A imes e_A ig) - ig( {}_\infty r_A imes e_A ig)^2 / 6 ig) \ \\ {}_5 \widehat{N}_x &= 2.5 ig( \widehat{N}_x + \widehat{N}_{x+5} ig) \end{aligned}$$

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#### Synthetic Extinct Generation method - steps

• Step 5: Estimate the number of people aged x, x+5 during the period between the two censuses, from the census populations

$$_5N_x = (t_2 - t_1) \left( _5N_x(t_1) imes _5N_x(t_2) 
ight)^{1/2}$$

• Step 6: Calculate the ratios of estimated over observed  $_5N_x$  as well as and ratios of estimated over observed  $_{A-x}N_x$ .

$$\frac{5\widehat{N}_x}{5N_x}$$
 and  $\frac{A-x\widehat{N}_x}{A-xN_x}$ 

### Synthetic Extinct Generation method - steps

- Step 7: Estimate the completeness of reported deaths
  - $\bullet$  Adjust  $\delta$  if necessary, using data/solver in spreadsheet
  - Decide about age range of ratios
- More complex procedure using iteration is described in IUSSP volume.

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# Synthetic Extinct Generation method - limitations

- ullet Incorrect estimate of relative coverage of the censuses  $\delta$
- Exaggeration of reported age
- Age misstatement in population estimates and age-specific miscounting

#### GGB vs. SEG

- Both methods robust to age misreporting
- GGB more sensitive to coverage errors that change with age
- SEG sensitive to time change in census coverage
  - Importance of using  $\delta$  adjustment
- Fit using 5+ to 65+ better than 15+ to 55+
- Both GGB and SEG are very sensitive to net migration
- If little migration: Use GGB first, estimate  $\delta$ , then apply SEG
- If significant migration: Apply both GGB and SEG, fit 30+ to 65+, and average results of both methods